

---

# Effect of Skew on Support Length Demands of Bridges with Seat-Type Abutments

---

Suiwen Wu and Ian G. Buckle

Department of Civil and Environmental Engineering  
University of Nevada, Reno, United States of America

Third International Bridge Seismic Workshop,  
University of Washington, Seattle, October 1-4, 2019



# Outline

---

- Background (seismic damage to skew bridges)
- Skew factors in current specifications and manuals
- Shake table experiment
- Experimental validation of a numerical model
- Parameter study
- Comparison of skew factors
- Summary and Conclusions
- Recommendations
- Acknowledgements

# Background: seismic damage to skew bridges

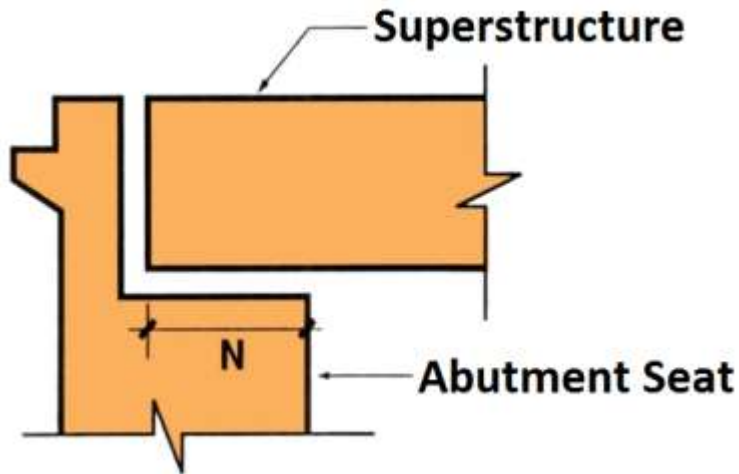


I-5 Overpass at Gavin Canyon (66°)  
1994 Northridge Earthquake, CA



Hospital Overpass  
2010 Maule Earthquake, Chile

# Skew factors in current specifications and design manuals



**In AASHTO:**

$$N_{\theta} = (8 + 0.02L + 0.08H)(1 + 0.000125\theta^2)$$

*i. e.*,  $N_{\theta} = N_0(1 + 0.000125\theta^2)$

$$f(\theta) = \frac{N_{\theta} - N_0}{N_0} = 0.000125\theta^2$$

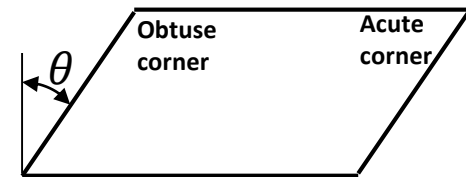
where:

$f(\theta)$  = skew factor, which is the ratio of additional support length due to skew to support length of straight bridges

$N_0$  = minimum support length for straight bridges (in)

$N_{\theta}$  = minimum support length for skew bridges (in)

$\theta$  = skew angle ( $^{\circ}$ ), which is measured from the line perpendicular to the longitudinal axis to the centerline of the support



# Skew factors in current specifications and design manuals

**FHWA Retrofit Manual (Buckle et al. 2006)  
& Caltrans SDC 2.0**

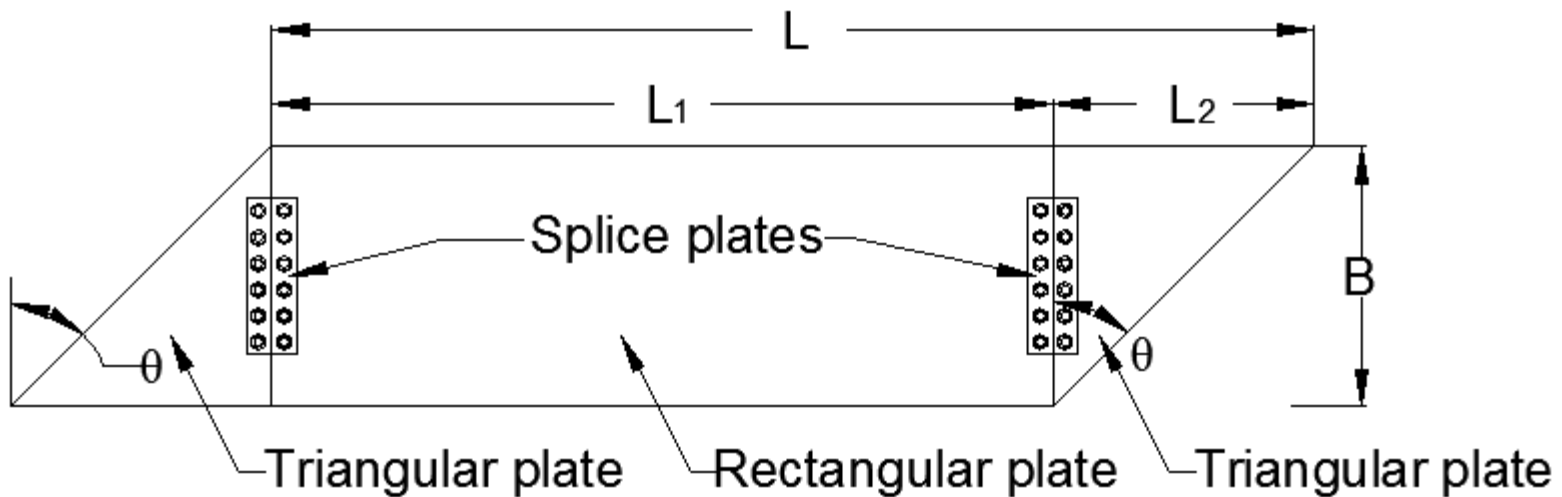
$$f(\theta) = \frac{1 - \cos\theta}{\cos\theta}$$



Note that these skew factors are based on engineering judgment.

# Shake table experiments - bridge models

Cases	$\theta$ ( $^{\circ}$ )	B (ft)	L (ft)	L (in)	$L_1$ (in)	$L_2$ (in)	L/B	h(in)	W (kips)
Case 1	0	3.5	10.50	126	126	0.00	3.00	2.0	3.3
Case 2	30	3.5	12.50	150	126	24	3.57	2.0	4.1
Case 3	45	3.5	14.00	168	126	42	4.00	2.0	4.6
Case 4	60	3.5	16.50	198	126	72	4.71	2.0	5.3

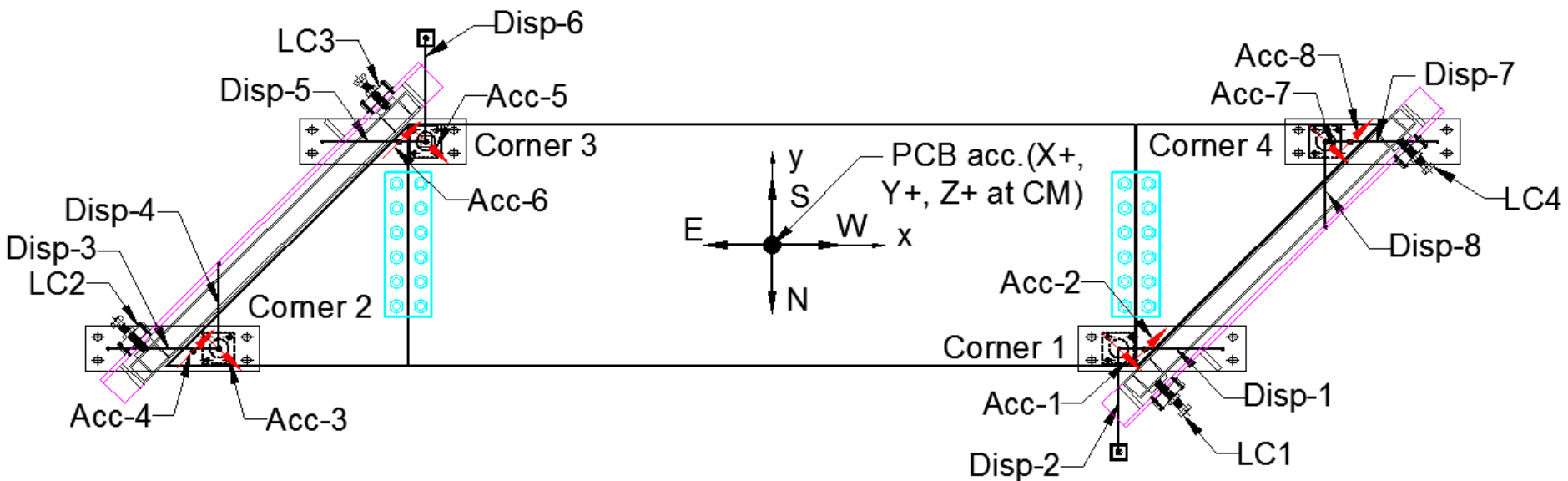


Model scale =  $3.5/40 \approx 1/10$

# Shake table experiments - instrumentation

Transducers used to measure:

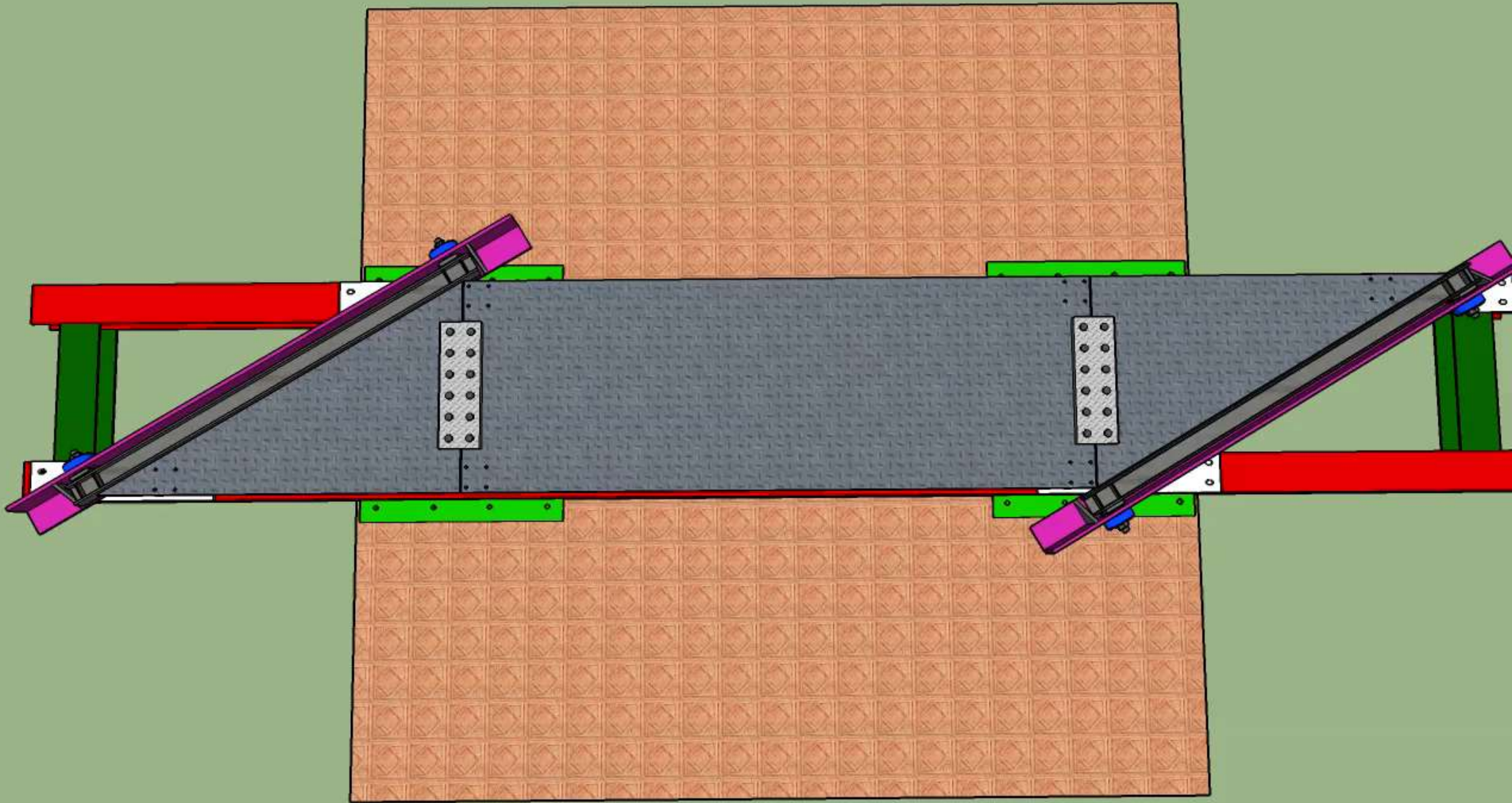
- displacements
- accelerations and
- impact forces between bridge deck and abutments



Plan view of instrumentation for 45° model (other models similar)



# Schematic of skew bridge model on shake table

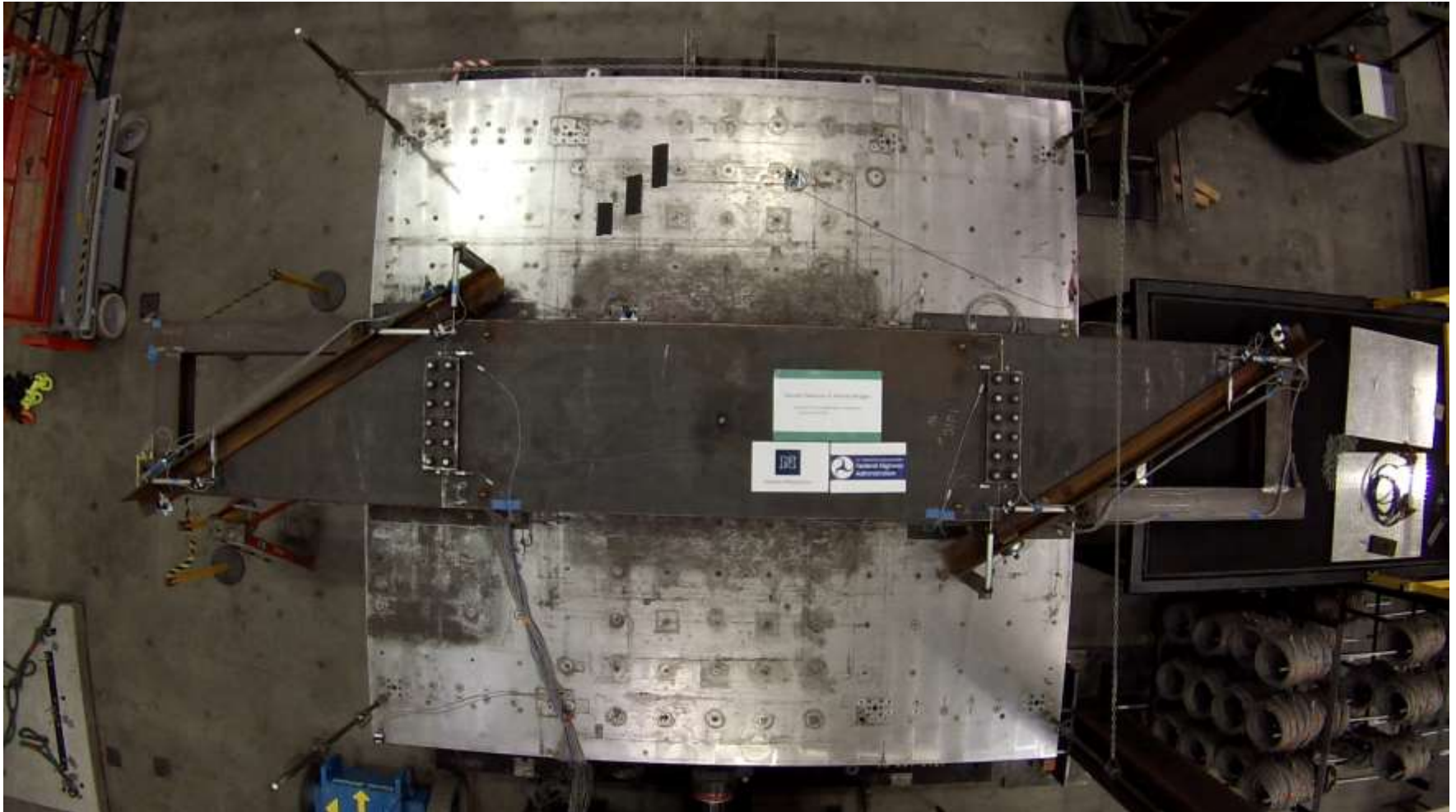




# Shake table experiments - test matrix

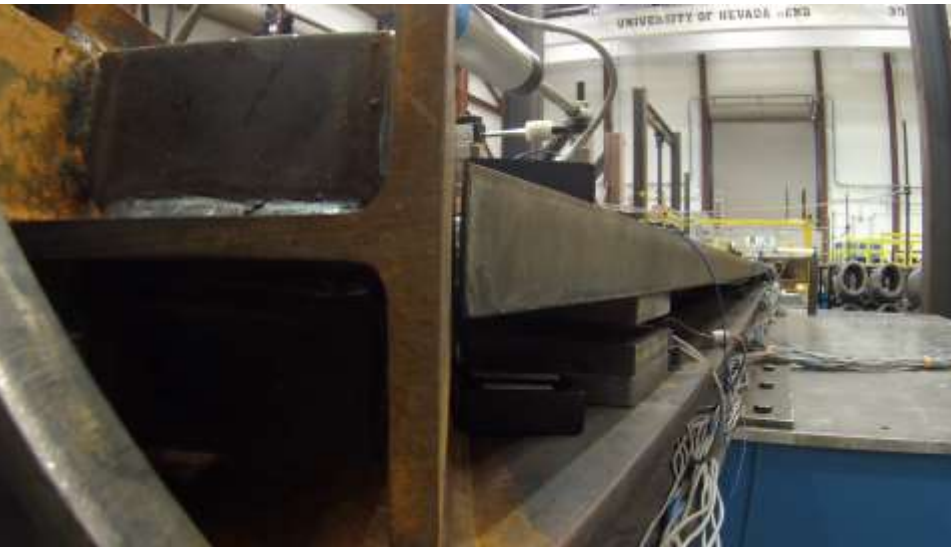
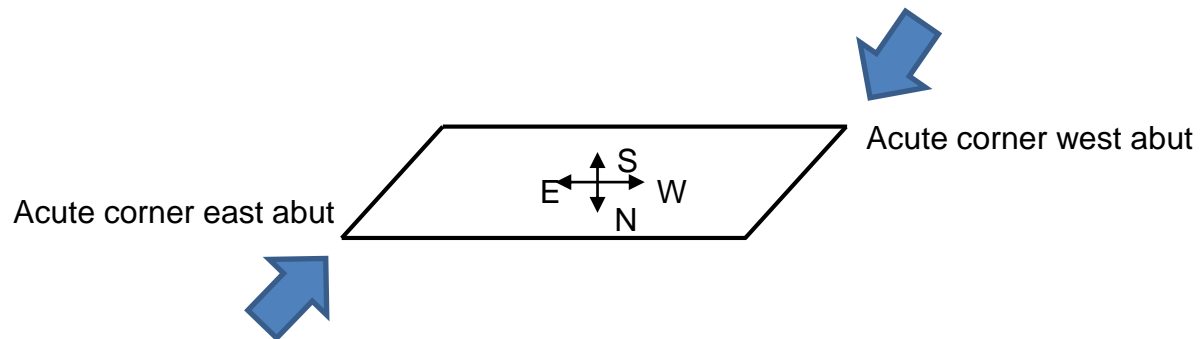
<b>Skew, <math>\theta</math></b>	$0^{\circ}$ , $30^{\circ}$ , $45^{\circ}$ , $60^{\circ}$
<b>Abutment gap</b>	0", 1/16", 1/8", 3/16", 1/4" (0 to 3" in prototype bridges)
<b>EQ record</b>	El Centro (1940), Century City (1994), Sylmar (1994)
<b>EQ levels</b>	50%DE, 75%DE, 100%DE, 150%DE, 200%DE,
<b>EQ input direction</b>	Transverse only, Longitudinal only, Biaxial
<b>Total runs</b>	876

# Shake table experiments (plan view)



$\theta=60^\circ$ , gap=1/8 in, SYL1994, biaxial input, 200%DE

# Shake table experiments (side views)



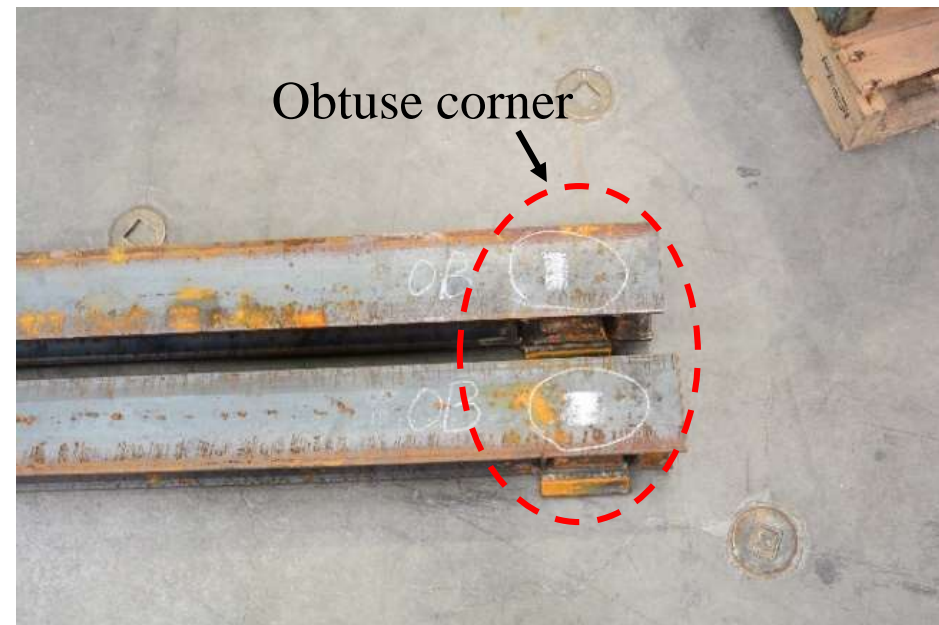
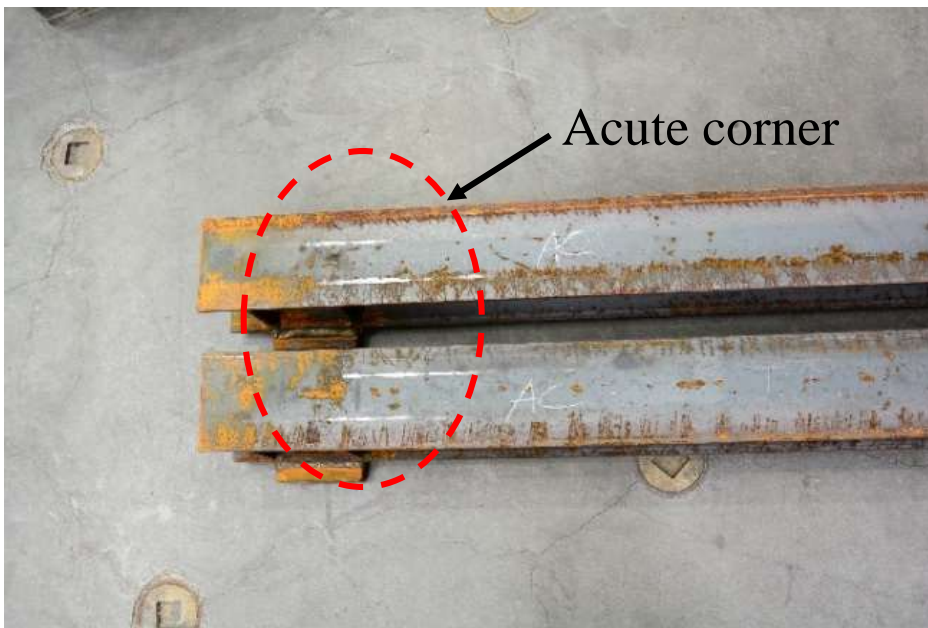
Acute corner east abutment



Acute corner west abutment

$\theta=60^{\circ}$ , gap=1/8 in, SYL1994, biaxial input, 200%DE

# Shake table experiments (face beams)



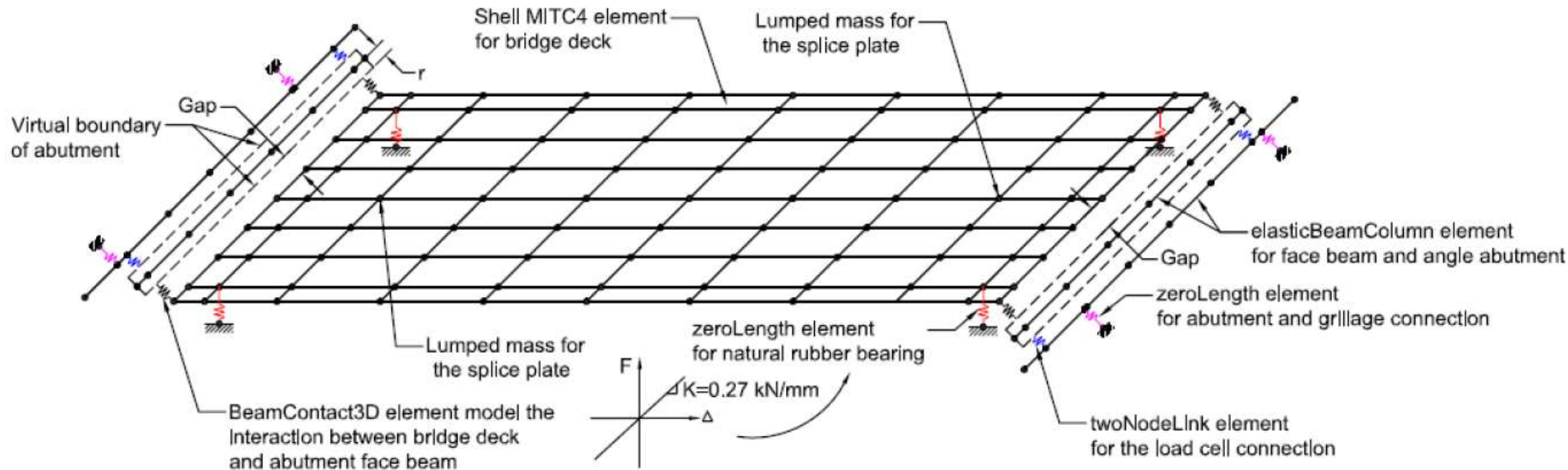
Abrasion marks on face beams from the 60° model (other models similar)

Complete dataset of this experiment is stored in:

- Wu, S., Buckle, I.G., Itani, A.M., and Istrati, D. (2019). “Experimental datasets from large-scale shake table experiments on skew bridges.” <https://doi.org/10.17605/OSF.IO/2Q3DP>.



# Validation of the numerical model in OpenSEES



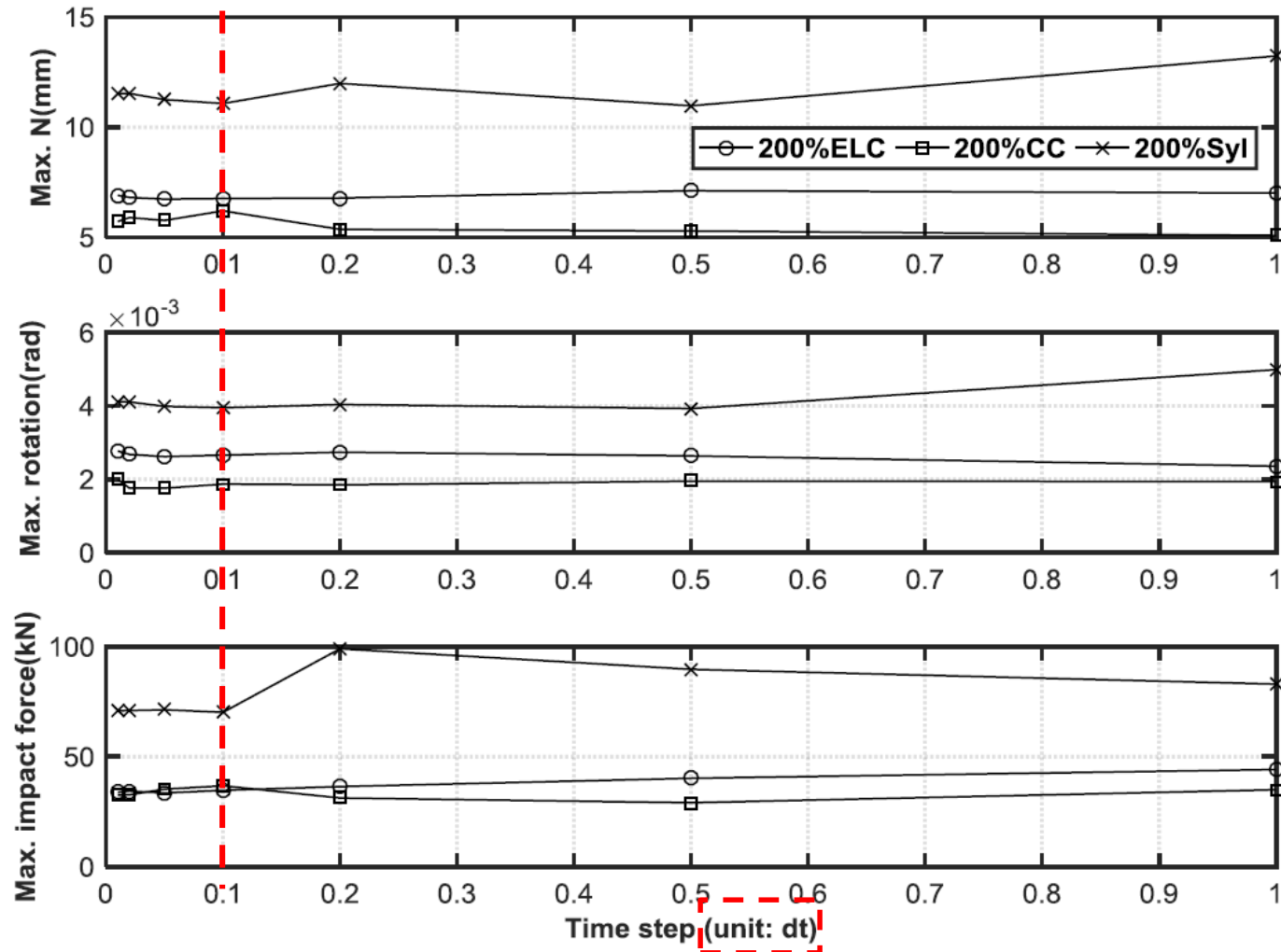
# Validation of the numerical model in OpenSEES

---

- Shell elements with distributed mass were used to model the bridge deck
- Elastomeric bearings were represented by linear springs based on the properties estimated from quick-release tests which are corresponding to 50% shear strain of the bearings
- “BeamContact3D” elements were used to model the gap, impact, and friction effects between deck and abutments. Friction coefficient = 0.3 for steel-on-steel.
- Damping assumed to be same in first translational and first rotational modes, and based on the quick-release tests (50% shear strain of the bearings).

# Validation of the numerical model in OpenSEES

- $dt=1/256$  sec
- Results were converged when time step reduced to  $dt/10$
- $Dt/10$  was used for the analysis.

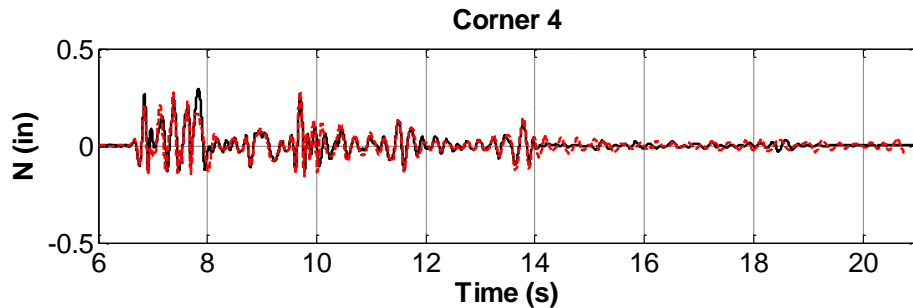
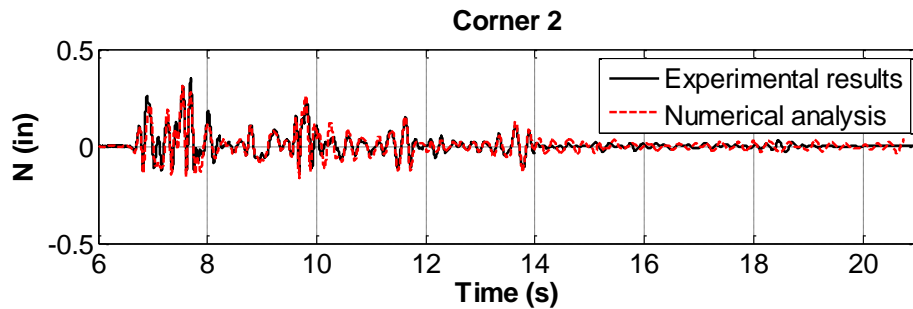
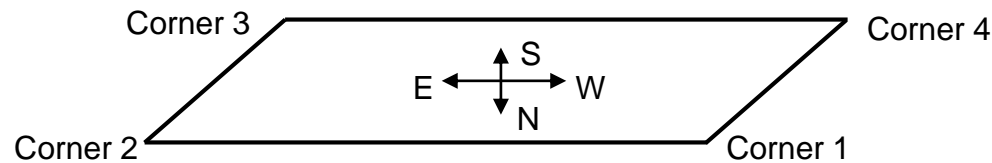


Maximum response quantities vs time step dt



# Validation of the numerical model in OpenSEES

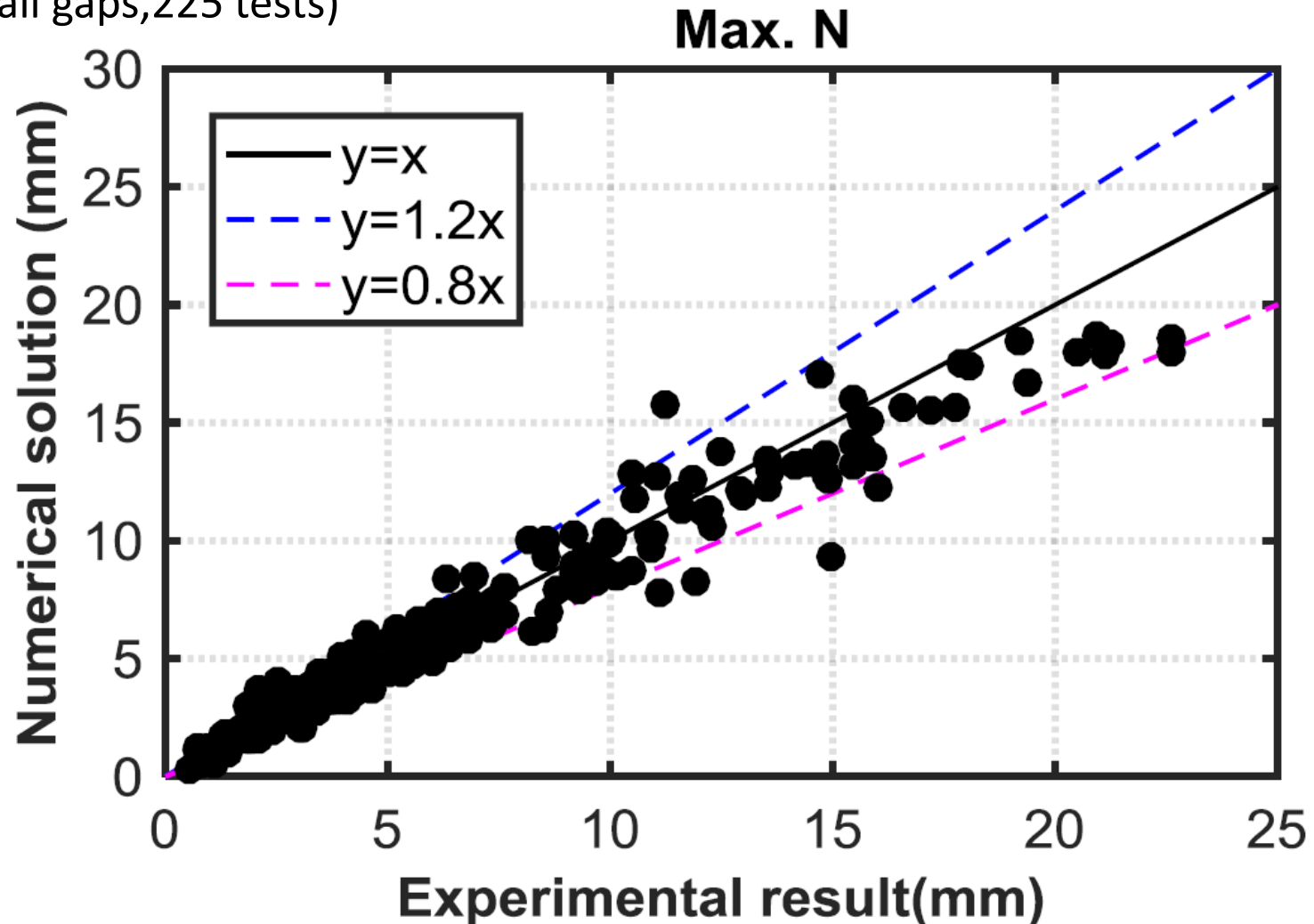
Run 125, 45<sup>0</sup> model: Gap=1/8 in, 200%DE, El Centro, biaxial input:



Normal displacements at acute corners

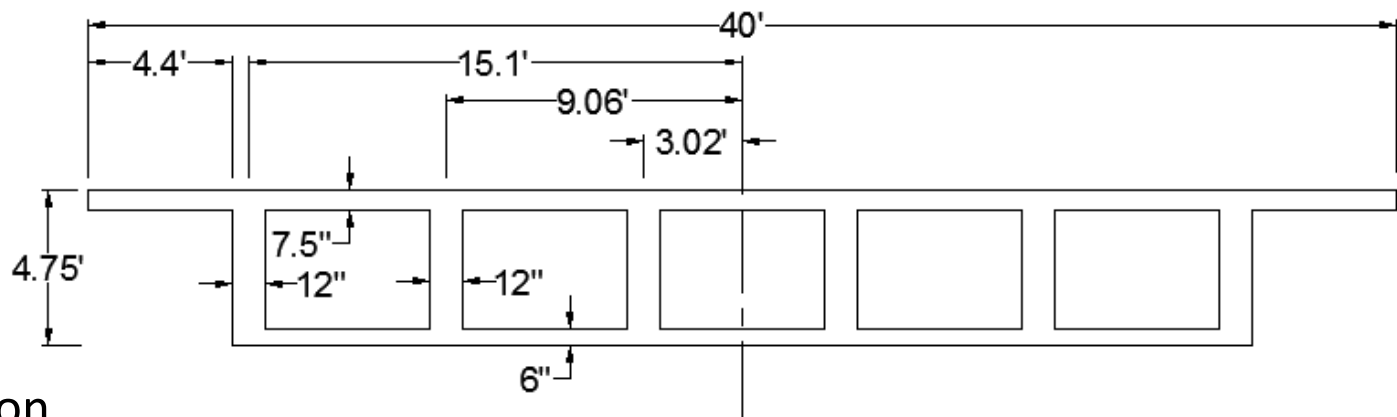
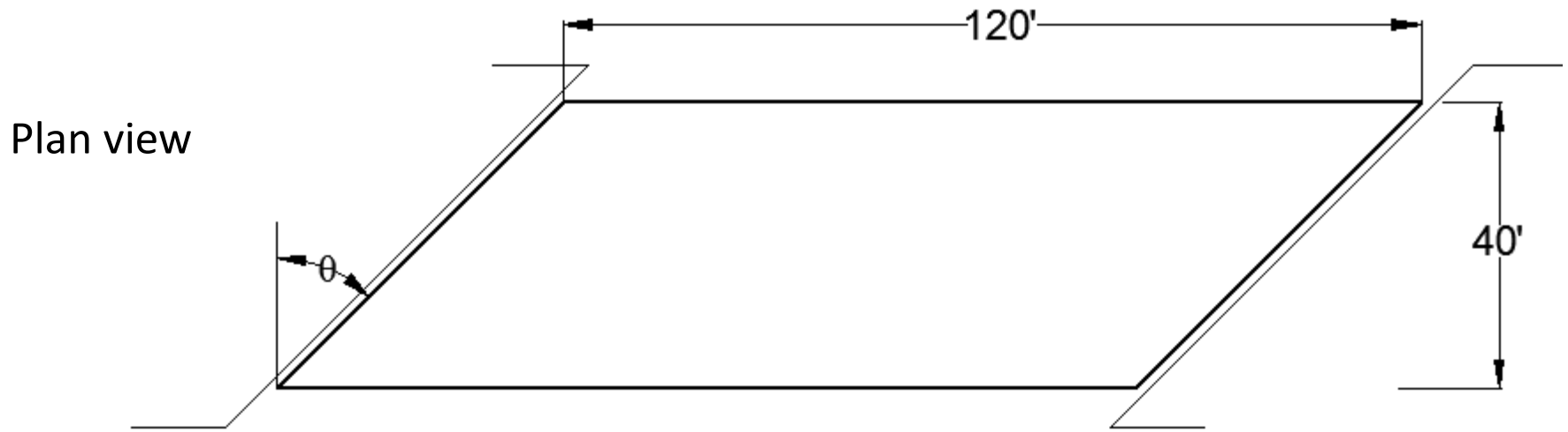
# Validation of the numerical model in OpenSEES

Maximum normal displacement (numerical vs experimental results) for 60° model (all EQs and all gaps, 225 tests)



# Parameter study - basic bridge geometry

Prototype bridge: single-span, seat-type abuts,  $T = 0.85s$ ,  $\Delta_{temp} = 1.05$  in



Cross section

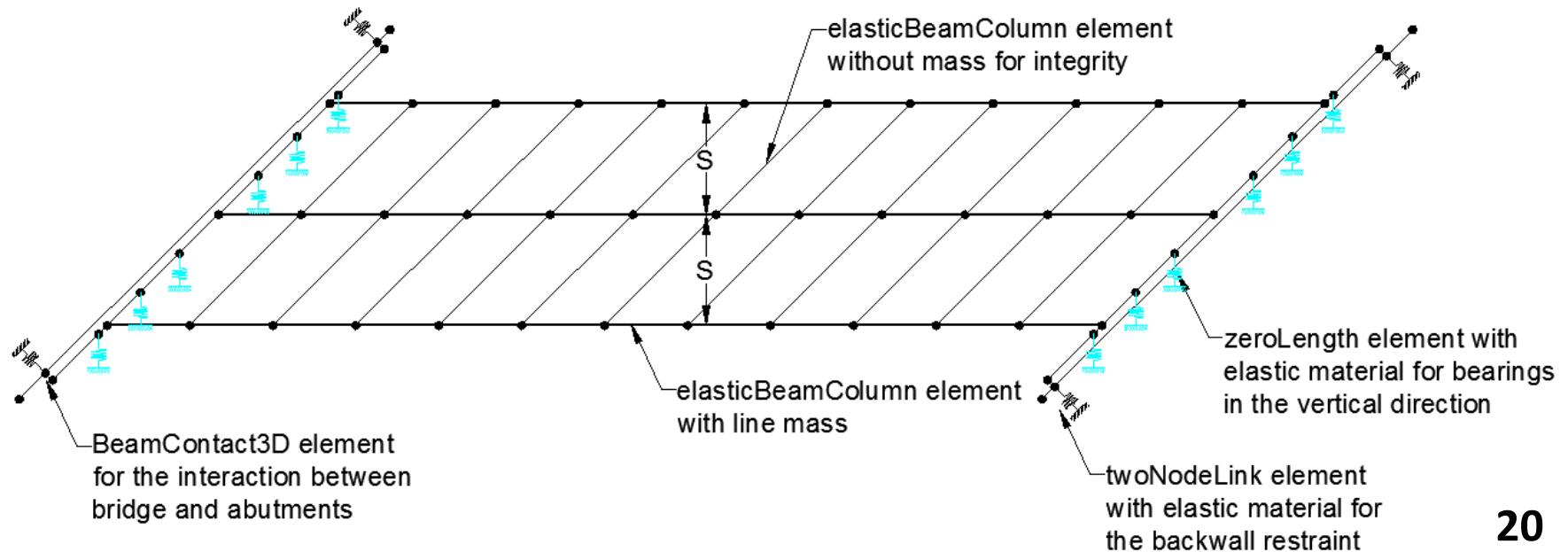
# Parameter study – analysis cases

For each configuration, skew varied from  $0^{\circ}$  to  $60^{\circ}$  in steps of  $5^{\circ}$

Group 1 (Constant B=40 ft)										
Case #	L (ft)	B (ft)	L/B	d (ft)	Gap (in)	N <sub>0</sub> from AASHTO (in)	Total weight (kips)	K (kip/in /bearing)	# of bearings	T (s)
1	100	40	2.5	4.5	0.5	15	913	10.76	12	0.85
2	120	40	3	4.75	0.5	15.6	1122	13.23	12	0.85
3	140	40	3.5	6.3	0.75	16.2	1505	17.73	12	0.85
4	160	40	4	7.2	0.75	16.8	1849	21.79	12	0.85
5	180	40	4.5	8.1	1	17.4	2226	26.23	12	0.85
6	200	40	5	9	1	18	2636	31.06	12	0.85
Group 2 (Constant L=120 ft)										
Case #	L (ft)	B (ft)	L/B	d (ft)	Gap (in)	N <sub>0</sub> from AASHTO (in)	Total weight (kips)	K (kip/in /bearing)	# of bearings	T (s)
7	120	48	2.5	4.75	0.5	15.6	1350	14	14	0.85
8	120	40	3	4.75	0.5	15.6	1122	13	12	0.85
9	120	34	3.5	4.75	0.5	15.6	936	13	10	0.85
10	120	30	4	4.75	0.5	15.6	855	12	10	0.85
11	120	27	4.5	4.75	0.5	15.6	729	13	8	0.85
12	120	24	5	4.75	0.5	15.6	668	12	8	0.85

# Parameter study-OpenSEES model

- Rigid abutment assumed
- BeamContact3D element used to model impact and friction between bridge and abutment
- Coefficient of friction taken as 1.0 for concrete-on-concrete
- 5% damping in first translational and first rotational modes



# Parameter study – ground motions

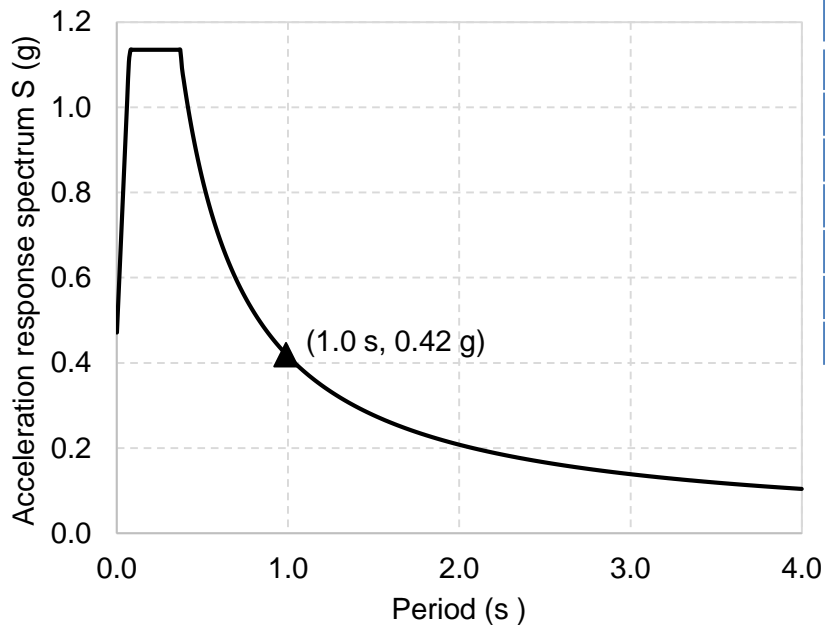
## Far field ground motions

Record #	EQ	Year	Station	Distance (km)
1	Imperial Valley	1940	El Centro Array #9	6.09
2	San Fernando	1971	Castaic	22.63
3	Friuli, Italy	1976	Tolmezzo	15.82
4	Northridge	1994	Sun Valley	10.05
5	Northridge	1994	Century City	23.41
6	Loma Prieta	1989	Anderson Dam	20.26
7	Imperial Valley	1979	El Centro Array #11	12.56

## Near field ground motions

Record #	Record Name	Year	Station Name	Distance (km)
1	Imperial Valley	1979	El Centro Array #3	12.85
2	Northridge	1994	Sylmar	5.3
3	Loma Prieta	1989	Gilroy Array #2	11.07
4	Landers	1992	Lucerne	2.19
5	Northridge	1994	Pacoima Dam	7.01
6	Duzce, Turkey	1999	IRIGM 487	2.65
7	Chi-Chi, Taiwan	1999	TCU053	5.95

Design response spectrum



Design response spectrum for  
**seismic zone 3**

Average results from 7 ground motions used to draw conclusions

# Parameter study $-f(\theta)$

For purpose of this study, take:

$$N_{\theta} = n_{\theta} + a$$

$$N_0 = n_0 + a$$

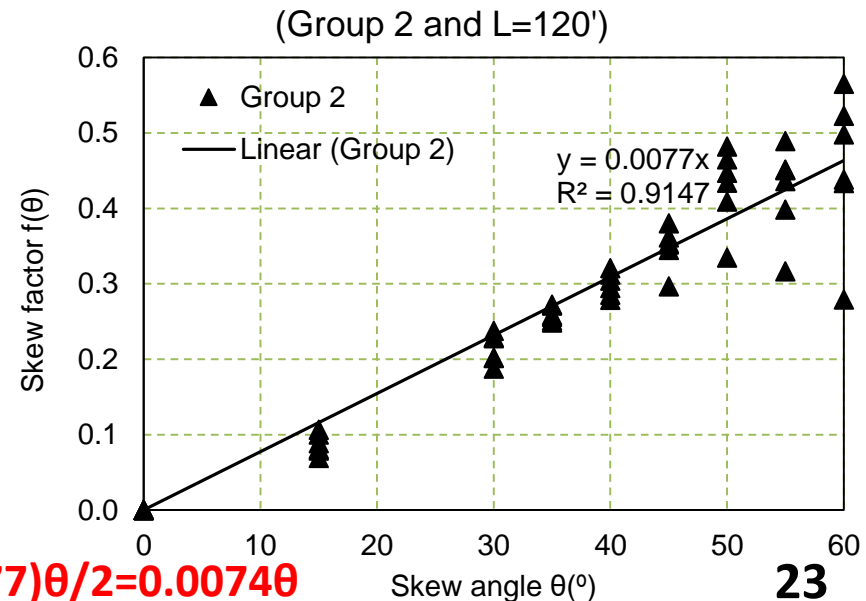
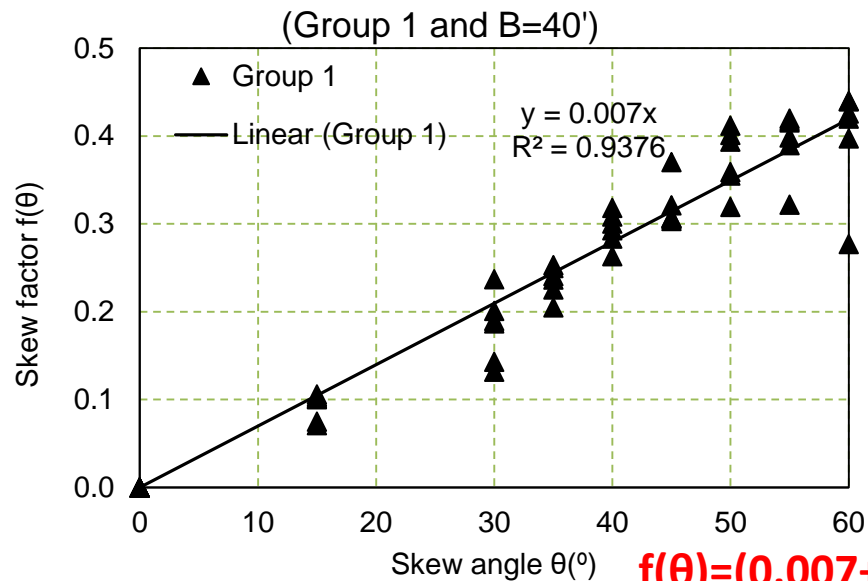
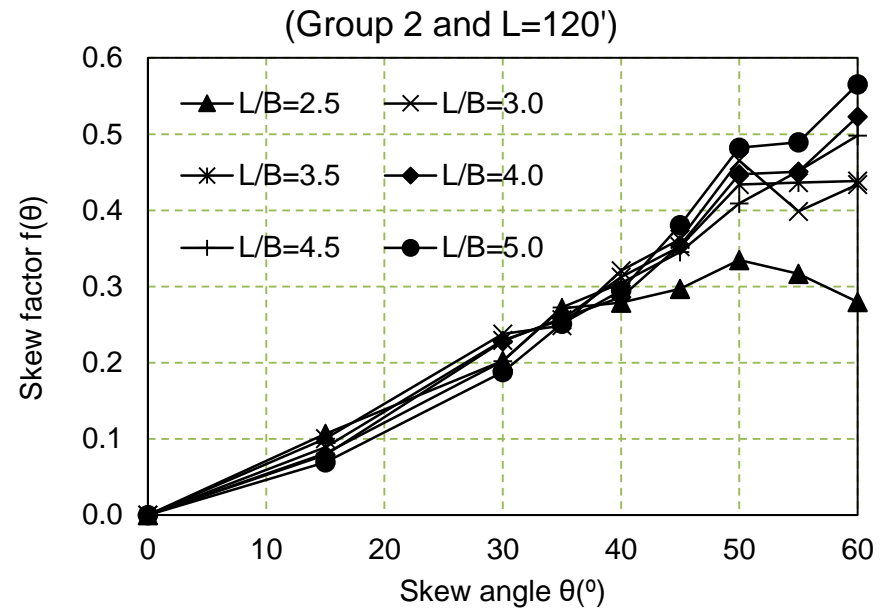
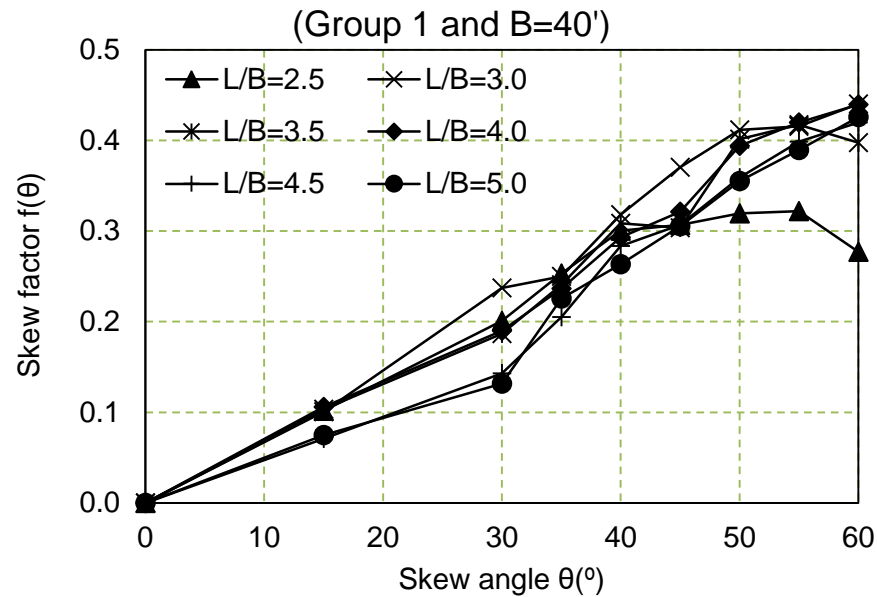
where  $n_{\theta}$  and  $n_0$  are the calculated displacement demands normal to the abutments at the supports of skewed and straight bridges respectively, and  $a$  is allowance for the cover concrete at the edge of the seat.

$$\begin{aligned} a &= 76.2 \text{ mm (3.0 in)} (\text{cover}) + 25.4 \text{ mm (1.0 in)} \text{ rebar diameter} \\ &= 101.6 \text{ mm (4.0 in)} \end{aligned}$$

$$\text{Then skew factor, } f(\theta) = \frac{N_{\theta} - N_0}{N_0} = \frac{n_{\theta} - n_0}{n_0 + 101.6}$$



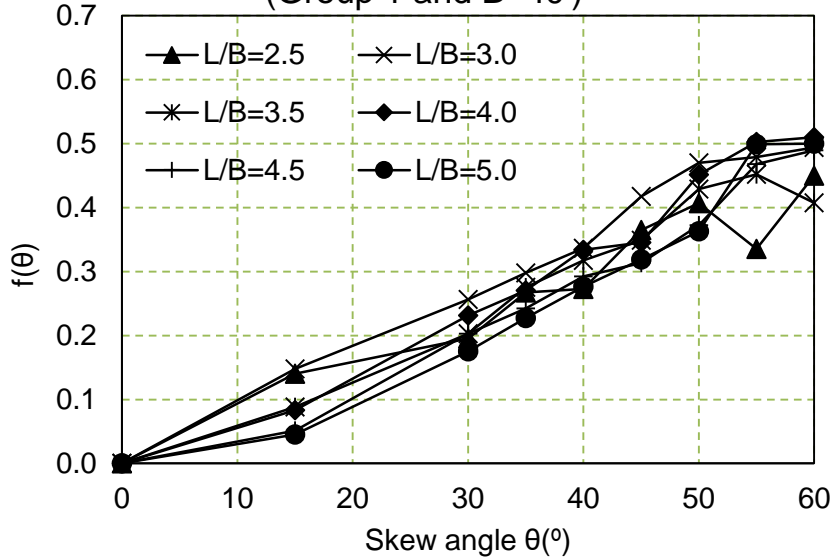
# Parameter study $-f(\theta) = \delta N / N_0$ (far-field GMs)



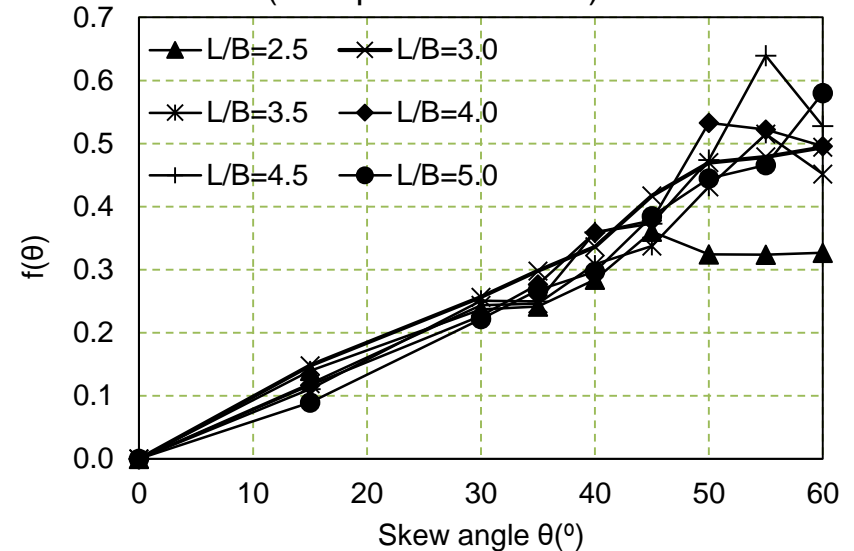
$$f(\theta) = (0.007 + 0.0077)\theta / 2 = 0.0074\theta$$

# Parameter study $-f(\theta) = \delta N / N_0$ (Near-field GMs)

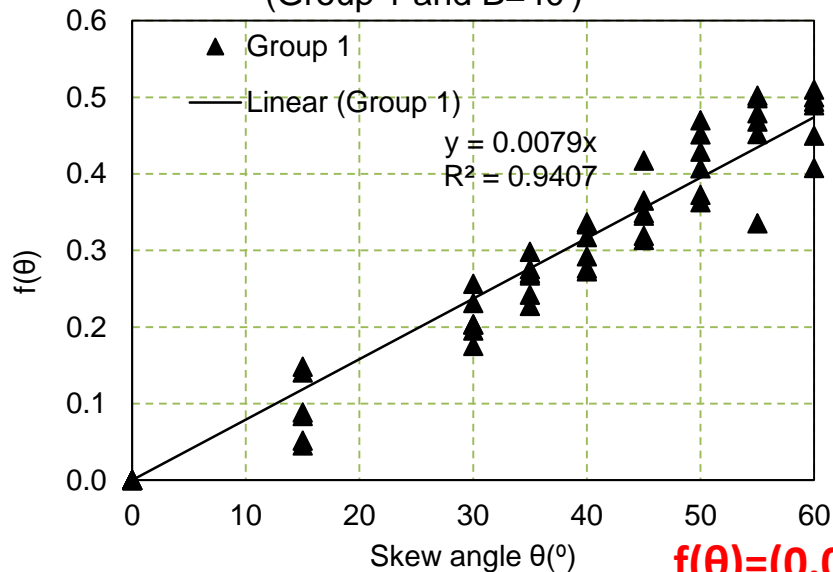
(Group 1 and B=40')



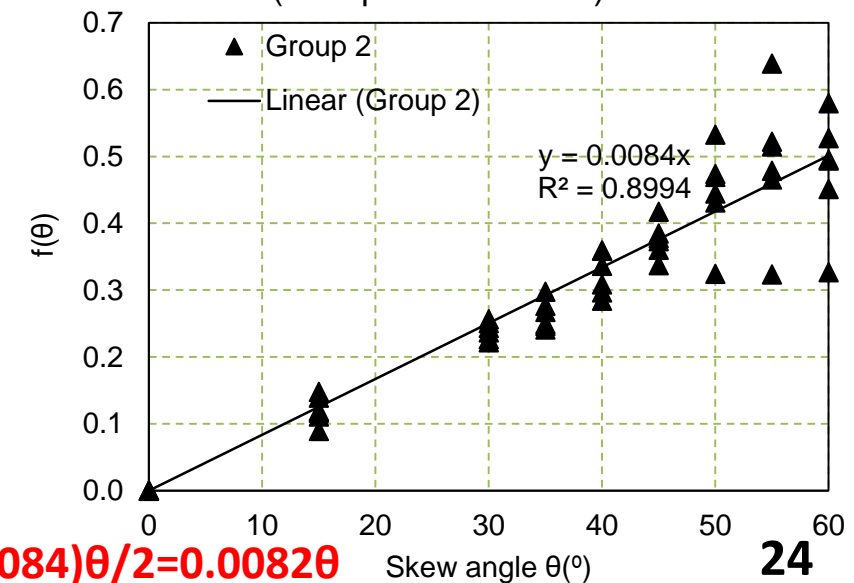
(Group 2 and L=120')



(Group 1 and B=40')

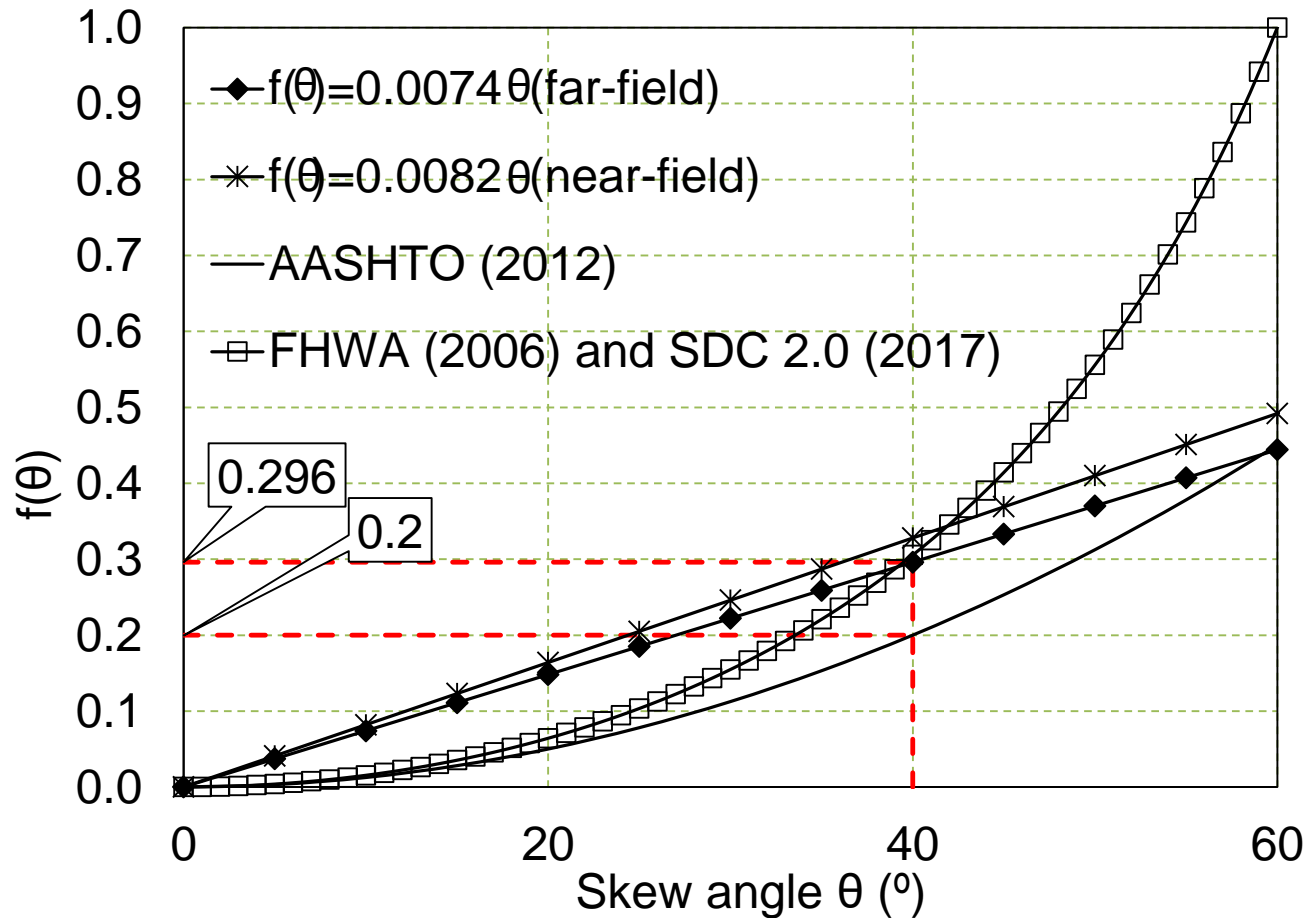


(Group 2 and L=120')



$f(\theta) = (0.0079 + 0.0084)\theta / 2 = 0.0082\theta$

# Comparison of skew factors



Skew factor  $f(\theta) = (N_\theta - N_0) / N_0$

At  $40^\circ$  skew,  $f_{recomm} / f_{AASHTO} = 0.296 / 0.2 = 1.5$

# Summary and conclusions – analytical investigation

---

- The numerical models with and without abutment pounding, show good correlation with the experimental results and therefore can be used with confidence to investigate the seismic response of skew bridges
- The skew factor  $f(\theta)$  for the minimum support length increases linearly with skew angle from  $0^\circ$  to  $60^\circ$  for both near-field and far-field ground motions.
- The skew factor for the minimum support length of skewed bridges is larger for near-field ground motions than that for far-field ground motions.
- The skew factor in AASHTO Specifications ( $0.000125\theta^2$ ) is unconservative particularly for skew angles in the range 15 to 45 degrees.

# Recommendations

---

- $f(\theta) = 0.0074\theta$  (far-field bridges)
- $f(\theta) = 0.0082\theta$  (near-field bridges)

# Acknowledgements

---

- Financial support provided by:
  - Federal Highway Administration under Contract No. DTFH61-07-C-0031 with technical oversight provided by FHWA CORs:
    - Dr Wen-huei (Phillip) Yen
    - Mr Fred Faridazar, and
    - Ms Sheila Duwadi
- Technical assistance from Earthquake Engineering Lab provided by:
  - Patrick Laplace, Chad and Todd Lyttle

---

---

Thank you!

---

---



---

---

Any questions?

---

---